



Logic Programming



Facts



Example.

father, mother, male and female are predicates

father(terach, abraham).

father(terach, nachor).

father(terach, haran).

father(abraham, issac).

father(haran, lot).

father(haran, milcah).

father(haran, yiscah).

mother(sarah, issac).

male(terach).

male(abraham).

male(nachor).

male(haran).

male(issac).

male(lot).

female(sarah).

female(milcah).

female(yiscah).



Facts

Example.

$$0 < 1.$$

$$0 < 2.$$

$$1 < 2.$$

$$0 < 3.$$

$$1 < 3.$$

$$2 < 3.$$

Queries

father(terach, abraham).

father(terach, nachor).

father(terach, haran).

father(abraham, issac).

father(haran, lot).

father(haran, milcah).

father(haran, yiscah).

mother(sarah, issac).

male(terach).

male(abraham).

male(nachor).

male(haran).

male(issac).

male(lot).

female(sarah).

female(milcah).

female(yiscah).

Query: father(abraham, issac)? ✓

Queries

father(terach, abraham).

father(terach, nachor).

father(terach, haran).

father(abraham, issac).

father(haran, lot).

father(haran, milcah).

father(haran, yiscah).

mother(sarah, issac).

male(terach).

male(abraham).

male(nachor).

male(haran).

male(issac).

male(lot).

female(sarah).

female(milcah).

female(yiscah).

Query: female(abraham)? ✗

Queries

father(terach, abraham).

father(terach, nachor).

father(terach, haran).

father(abraham, issac).

father(haran, lot).

father(haran, milcah).

father(haran, yiscah).

mother(sarah, issac).

male(terach).

male(abraham).

male(nachor).

male(haran).

male(issac).

male(lot).

female(sarah).

female(milcah).

female(yiscah).

Query: father(abraham, X)? X=issac.

father(abraham, lot)?, father(abraham, milcah)?, ...,
father(abraham, issac)?, ...

stops until an answer yes is given.

Universal Facts

likes(abraham, pomegranates).

likes(sarah, pomegranates).

.....



likes(X, pomegranates).

Conjunctive Queries

father(terach, abraham).

father(terach, nachor).

father(terach, haran).

father(abraham, issac).

father(haran, lot).

father(haran, milcah).

father(haran, yiscah).

mother(sarah, issac).

male(terach).

male(abraham).

male(nachor).

male(haran).

male(issac).

male(lot).

female(sarah).

female(milcah).

female(yiscah).

Query: father(haran, X), male(X)? X=lot.

Is there an X such that both ... ?

Rules

Rules are statements of the form:

$$A \leftarrow B_1 \wedge B_2 \wedge \dots \wedge B_n.$$

In Prolog,

$$A :- B_1, B_2, \dots, B_n.$$

Example.

$\text{son}(X, Y) :- \text{father}(Y, X), \text{male}(X).$

$\text{grandfather}(X, Y) :- \text{father}(X, Z), \text{father}(Z, Y).$

Logic Program

Facts $\mathcal{F}$, rules $\mathcal{R}$ and a query Q :

$$\mathcal{F}, \mathcal{R} \models Q ?$$

Is Q the logical consequence of $\mathcal{F}$ and $\mathcal{R}$?

Program:

father(abraham, issac).	male(issac).
father(haran, lot).	male(lot).
father(haran, milcah).	female(milcah).
father(haran, yiscah).	female(yiscah).
son(X, Y) :- father (Y, X), male(X).	
daughter(X, Y) :- father(Y, X), female(X).	
son(lot, haran)?	

Recursive Programming

`natural_number(X) : X is a natural number.`



`natural_number(0).`

`natural_number(s(X)) :- natural_number(X).`

Example - Arithmetic

$X \leq Y$: X and Y are natural numbers, s.t.,
 X is less than or equal to Y .



$0 \leq X$:- natural_number(X).

$s(X) \leq s(Y)$:- $X \leq Y$.

natural_number(0).

natural_number($s(X)$) :- natural_number(X).

Example - Arithmetic

$\text{plus}(X, Y, Z)$: X, Y and Z are natural numbers, s.t.,
 Z is the sum of X and Y .



$\text{plus}(0, X, X) \text{ :- } \text{natural_number}(X).$

$\text{plus}(s(X), Y, s(Z)) \text{ :- } \text{plus}(X, Y, Z).$

$\text{natural_number}(0).$

$\text{natural_number}(s(X)) \text{ :- } \text{natural_number}(X).$

Example - List Concatenation

$\text{cat}(X, Y, Z)$: X , Y and Z are lists, s.t.,
 Z is the concatenation, i.e., $Z = [X|Y]$.



$\text{cat}([], Y, Y)$.

$\text{cat}([V|X], Y, [V|Z]) \text{ :- } \text{cat}(X, Y, Z)$.

Example - List Concatenation

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$\text{cat}([V|X], Y, [V|Z]) \text{ :- } \text{cat}(X, Y, Z)$.

$\text{cat}([1, 2], [3, 4], L)?$ $L = [1, 2, 3, 4]$.

Example - List Concatenation

$\text{cat}(X, Y, Z)$: X , Y and Z are lists, s.t.,
 Z is the concatenation, i.e., $Z = [X|Y]$.



$\mathcal{F}$: $\text{cat}([], Y, Y)$.

$\mathcal{R}$: $\text{cat}([V|X], Y, [V|Z]) \text{ :- } \text{cat}(X, Y, Z)$.

Q : $\text{cat}([1, 2], [3, 4], L)?$

$\mathcal{F}, \mathcal{R} \models Q?$

$\text{cat}([], [3,4], [3,4])$



$\text{cat}([2], [3, 4], [2, 3, 4])$



$\text{cat}([1, 2], [3, 4], [1, 2, 3, 4])$

Search

- Idea: To solve a query Q ,
 - If Q is a fact in the program, then done
 - Else, if $Q :- Q_1, \dots, Q_n$ is a rule in the program, solve $Q_1 \dots Q_n$.
 - Else, give up on this query.

"What" vs "How"

- Declarative vs Procedural Programming
- Procedural programming
 - The programmer has to specify how to get the output for the range of required inputs.
 - The programmer must know the appropriate algorithm.
- Declarative programming
 - Requires a more descriptive style.
 - The programmer must know what relationships hold between various entities.

Example - List Concatenation

In procedural style:

```
list procedure cat(list a,list b)
{
    list t = list u = copylist(a);
    while (t.tail != nil) t = t.tail;
    t.tail = b;
    return u;
}
```

In declarative style:

```
cat([], Y, Y).
cat([V|X], Y, [V|Z]) :- cat(X, Y, Z).
```

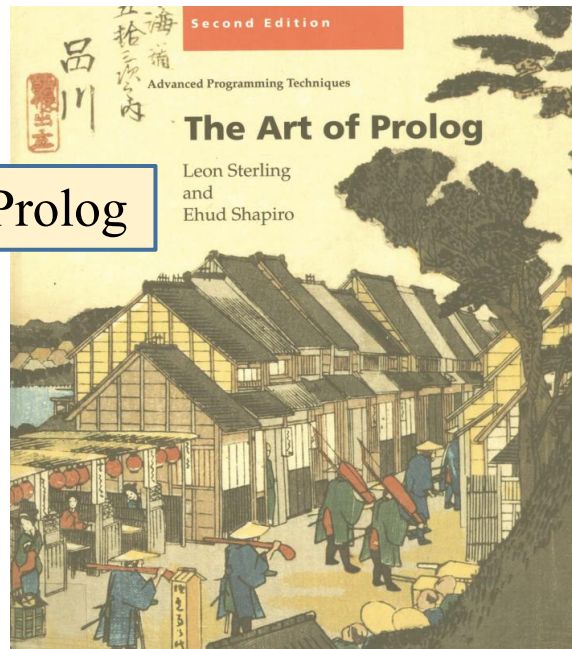


Logic Programming

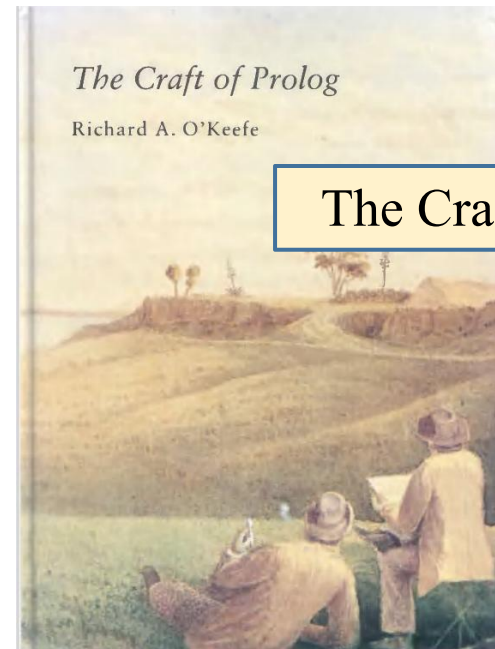
- A declarative style programming paradigm.
- Computation through logical deduction.
- Uses the language of logic to express data and programs.
- Most of current LP languages use first-order logic (FOL).
- **Prolog** – the most popular logic programming language.

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The Art of Prolog



The Craft of Prolog